

# CUSUM residual plots for assessing the fit of occupancy models.

Darryl I. MacKenzie



Proteus  
*Knowledge | Results | Data*

# Introduction

## Introduction

## Residual Defn.

## CUSUM Residual Plot

## Example

## Summary

- Few graphical diagnostics developed for occupancy models.

# Introduction

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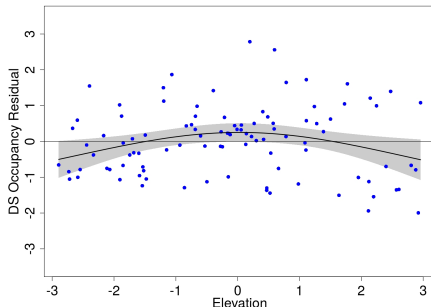
### Residual Defn.

### CUSUM Residual Plot

### Example

### Summary

- Few graphical diagnostics developed for occupancy models.
- Warton et al. (2017) suggested plots based on Dunn-Smyth residuals.



# Residual Definition

Introduction

Residual Defn.

CUSUM Residual  
Plot

Example

Summary

## ■ Definitions:

# Residual Definition

Introduction

Residual Defn.

CUSUM Residual  
Plot

Example

Summary

- Definitions:
  - $z_i$  = occupancy latent random variable.

# Residual Definition

Introduction

Residual Defn.

CUSUM Residual  
Plot

Example

Summary

- Definitions:
  - $z_i$  = occupancy latent random variable.
  - $h_{ij}$  = detection/nondetection data.

# Residual Definition

Introduction

Residual Defn.

CUSUM Residual  
Plot

Example

Summary

- Definitions:
  - $z_i$  = occupancy latent random variable.
  - $h_{ij}$  = detection/nondetection data.
  - $\psi_i = \Pr(\text{unit } i \text{ occupied})$ .

# Residual Definition

Introduction

Residual Defn.

CUSUM Residual  
Plot

Example

Summary

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# Residual Definition

Introduction

Residual Defn.

CUSUM Residual  
Plot

Example

Summary

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# Residual Definition

Introduction

Residual Defn.

CUSUM Residual  
Plot

Example

Summary

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- WARNING: explicit content to follow.

# Residual Definition

Introduction

Residual Defn.

CUSUM Residual  
Plot

Example

Summary

- For occupancy:

$$E [z_i | \mathbf{h}_i, \hat{\theta}] = 1, \text{ if at least one detection} \\ = \hat{\psi}_i^c, \text{ otherwise.}$$

$$\zeta_i = \frac{E [z_i | \mathbf{h}_i, \hat{\theta}] - \hat{\psi}_i}{\sqrt{\hat{\psi}_i (1 - \hat{\psi}_i)}}$$

# Residual Definition

Introduction

Residual Defn.

CUSUM Residual  
Plot

Example

Summary

- For detection:

$$\delta_{ij} = E \left[ z_i | \mathbf{h}_i, \hat{\theta} \right] \times \frac{h_{ij} - \hat{p}_{ij}}{\sqrt{\hat{p}_{ij} (1 - \hat{p}_{ij})}}.$$

# CUSUM Residual Plot

Introduction

Residual Defn.

**CUSUM Residual  
Plot**

Example

Summary

- Order residuals with respect to aspect of interest.
  - e.g., a potential covariate

# CUSUM Residual Plot

Introduction

Residual Defn.

**CUSUM Residual  
Plot**

Example

Summary

- Order residuals with respect to aspect of interest.
  - e.g., a potential covariate
- Calculate cumulative sum (CUSUM) of ordered residuals.

# CUSUM Residual Plot

Introduction

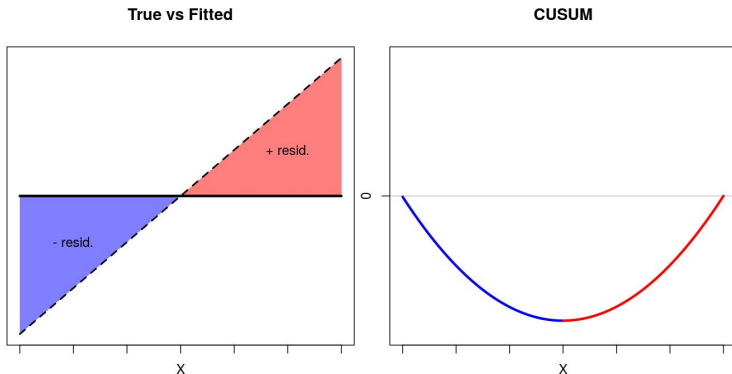
Residual Defn.

CUSUM Residual  
Plot

Example

Summary

## ■ Assess covariate relationships:



# CUSUM Residual Plot

Introduction

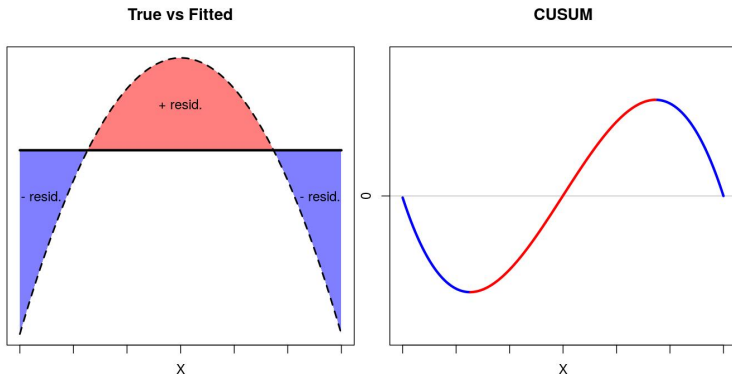
Residual Defn.

CUSUM Residual  
Plot

Example

Summary

## ■ Assess covariate relationships:





# CUSUM Residual Plot

Introduction

Residual Defn.

**CUSUM Residual  
Plot**

Example

Summary

- Use parametric bootstrap to assess 'typical' CUSUM curve for fitted model.
  - could be used to test model fit.

# CUSUM Residual Plot

Introduction

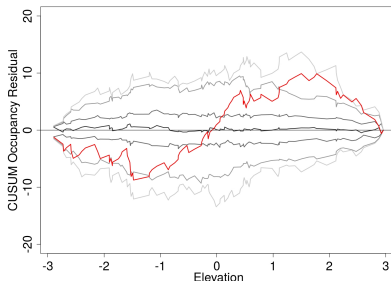
Residual Defn.

CUSUM Residual  
Plot

Example

Summary

- Use parametric bootstrap to assess 'typical' CUSUM curve for fitted model.
  - could be used to test model fit.
- Plot a percentile 'envelope' with respect to covariate values.



# Example

Introduction

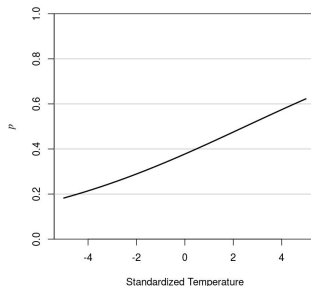
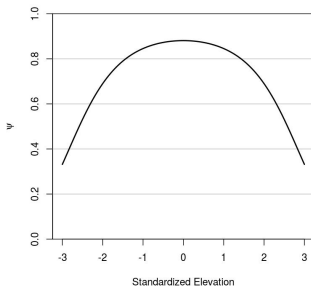
Residual Defn.

CUSUM Residual  
Plot

Example

Summary

## ■ Simulated data:



# Example

Introduction

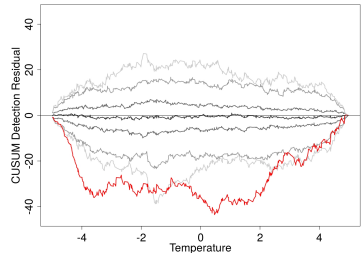
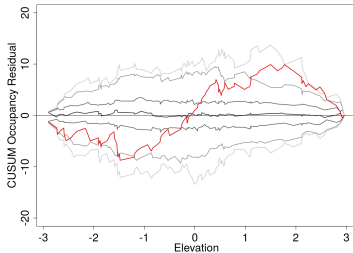
Residual Defn.

CUSUM Residual  
Plot

Example

Summary

■ Fitted model:  $\psi(\cdot)p(\cdot)$



# Example

Introduction

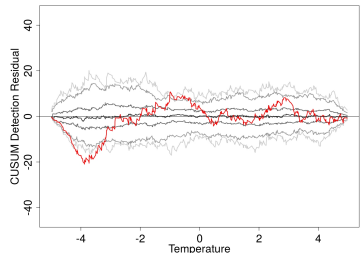
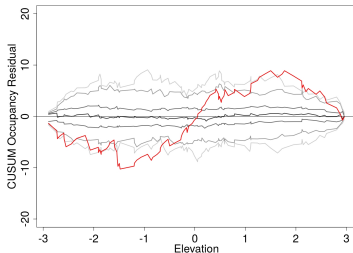
Residual Defn.

CUSUM Residual  
Plot

Example

Summary

- Fitted model:  $\psi(Elev.)p(Temp.)$



# Example

Introduction

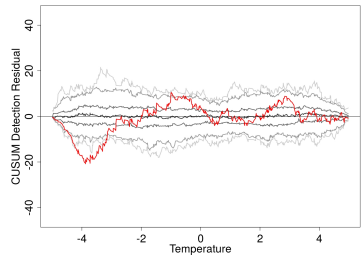
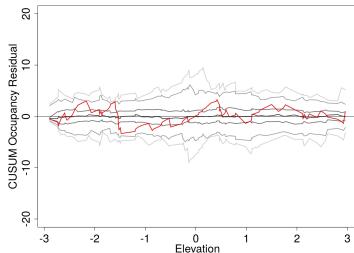
Residual Defn.

CUSUM Residual  
Plot

Example

Summary

- Fitted model:  $\psi(Elev. + Elev.^2)p(Temp.)$



# Summary

Introduction

Residual Defn.

CUSUM Residual  
Plot

Example

Summary

- Some ability to detect poor model fit.

# Summary

Introduction

Residual Defn.

CUSUM Residual  
Plot

Example

Summary

- Some ability to detect poor model fit.
- Suggest functional form for covariates.



# Summary

Introduction

Residual Defn.

CUSUM Residual  
Plot

Example

Summary

- Some ability to detect poor model fit.
- Suggest functional form for covariates.
- Works with categorical covariates.

# Summary

Introduction

Residual Defn.

CUSUM Residual  
Plot

Example

Summary

- Some ability to detect poor model fit.
- Suggest functional form for covariates.
- Works with categorical covariates.
- Other applications with (partially) latent variables.

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Introduction

Residual Defn.

CUSUM Residual  
Plot

Example

Summary

- Some ability to detect poor model fit.
- Suggest functional form for covariates.
- Works with categorical covariates.
- Other applications with (partially) latent variables.
  
- THANKS FOR LISTENING!